
Tango steps in a moving-horizon cabaret

Theory, concepts, heuristics and examples ...

Mazen Alamir

CNRS - University of Grenoble-Alpes



Outline

- 1 Non conventional NMPC Formulations
 - Economic MPC
 - Bringing the infinity closer
- 2 GPU-related topics
 - Some experiments
 - Use-case
- 3 Machine Learning-related topics
 - Stochastic NMPC by supervised clustering
 - ML-Model-based monitoring control updating period in NMPC
- 4 Discussion: Threats & suggestions for a data-dominated future

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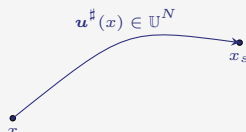
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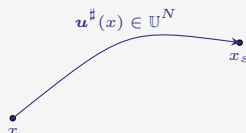
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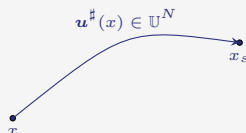
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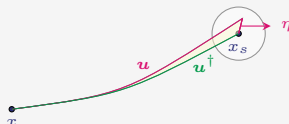
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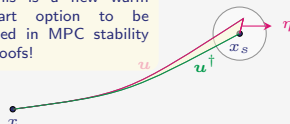
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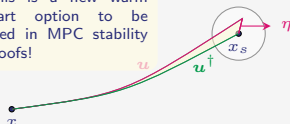
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A trajectory (\mathbf{x}, \mathbf{u}) is said to be **ϵ -quasi steady optimal** if and only if the following conditions hold for all k :

$$|\ell(x_k, u_k) - \ell_s| \leq \epsilon, \quad \Delta(x_k, u_k) \leq \epsilon$$

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Proposition. For any desired $\epsilon > 0$, \exists **sufficiently high** α, γ s.t the resulting closed-loop trajectory starting at $x_0 \in \mathbb{X}_0$ is asymptotically ϵ -quasi steady optimal.

Moreover, for dynamics that are obtained by time sampling, the size of the terminal region might be further reduced by **reducing the sampling period τ** .

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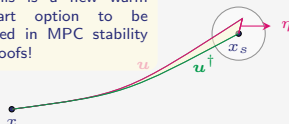
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MPC with exponentially increasing weight

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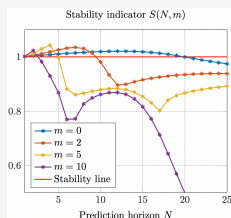
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Evolution of the highest module of closed-loop eigenvalues $S(N, m)$

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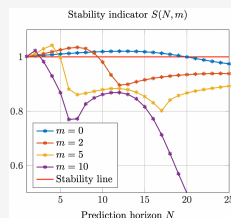
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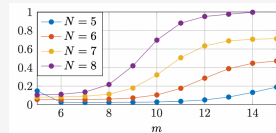
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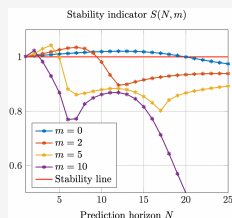
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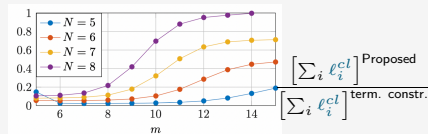
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The shorter N , the stronger is the advantage!

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 M.A Numerical investigation regarding ... Application to the control of real-life cryogenic plant, **NMPC workshop** 2018.

BRINGING INFINITY CLOSER!

MPC with exponentially increasing weight

Cost function

$$J(\mathbf{u}, \mathbf{x}) := \sum_{k=1}^N [k/N]^m \left[\varphi_m \ell_k^{\mathbf{u}} + (1 - \varphi_m) V_k^{\mathbf{u}} \right]$$

- ℓ is the stage cost of interest
- V is a local controlled Lyapunov function
- $\varphi(0) = 1$ and $\lim_{m \rightarrow \infty} \varphi_m = 0$
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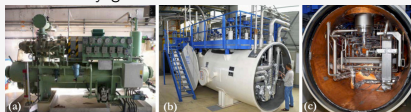
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Questions

- Q1.** Are we still minimizing the same cost?
- Q2.** Implication on the computation time!

Q1-Q2

Cryogenic station of CEA-INAC-SBT



$$\mathbf{x}^+ = A\mathbf{x} + B\mathbf{u} + G\mathbf{w}$$

$$\mathbf{y} = C\mathbf{x} + D\mathbf{u} \quad (\mathbf{x}, \mathbf{u}, \mathbf{y}, \mathbf{w}) \in \mathbb{R}^{24} \times \mathbb{R}^3 \times \mathbb{R}^3 \times \mathbb{R}$$

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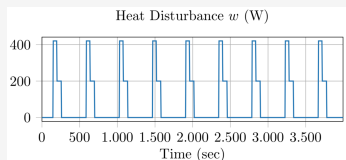
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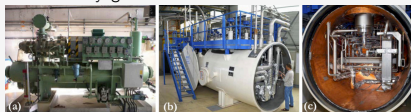
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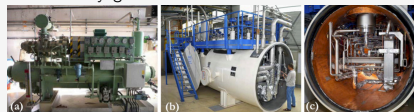
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$$\varepsilon_f \|\mathbf{x}_N\|^2 + \sum_{k=1}^N [k/N]^m \left[\|\mathbf{y}_k\|_{Q_y}^2 + \varepsilon \|\mathbf{x}_k\|^2 \right]$$

Controller Settings	ε_f	m	ε	N
Proposed Controller	0	3	0.01	10
Controller 1	0	0	0.01	10
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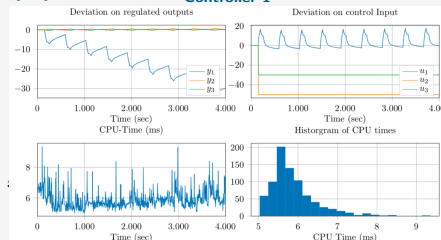
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Controller 1



$$\epsilon_f \|x_N\|^2 + \sum_{k=1}^N [k/N]^m \left[\|y_i\|_{Q_y}^2 + \epsilon \|x_i\|^2 \right]$$

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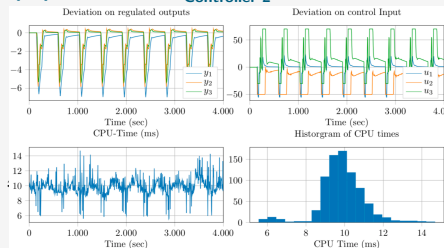
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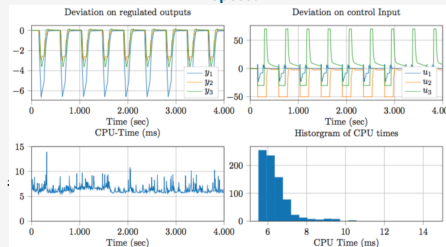
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Proposed



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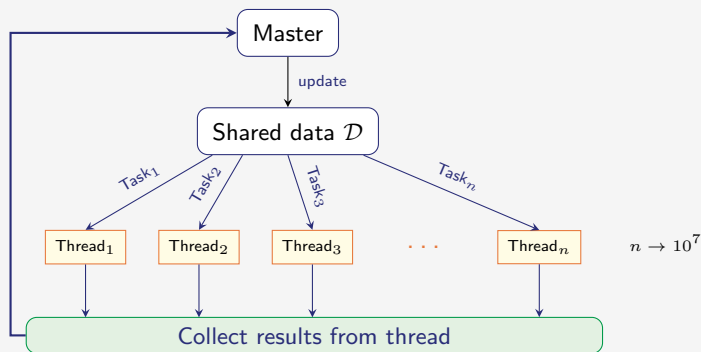
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- 1 Non conventional NMPC Formulations
- 2 GPU-related topics
- 3 Machine Learning-related topics
- 4 Discussion: Threats & suggestions for a data-dominated future



DISTRIBUTING THE COMPUTATION

GPU, FPGA ...



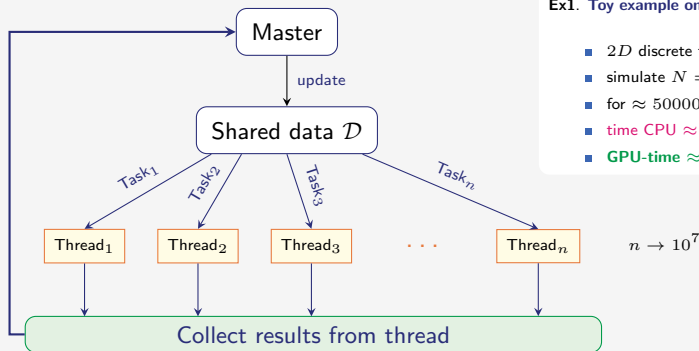
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Ex1. Toy example on GOOGLE-COLAB

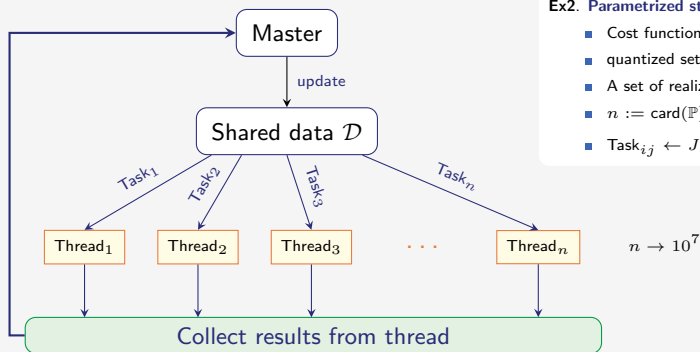
- 2D discrete time dynamics
- simulate $N = 20$ steps
- for ≈ 500000 initial states
- time CPU ≈ 2 min.
- GPU-time $\approx 400 \mu\text{-sec}$





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GPU, FPGA ...



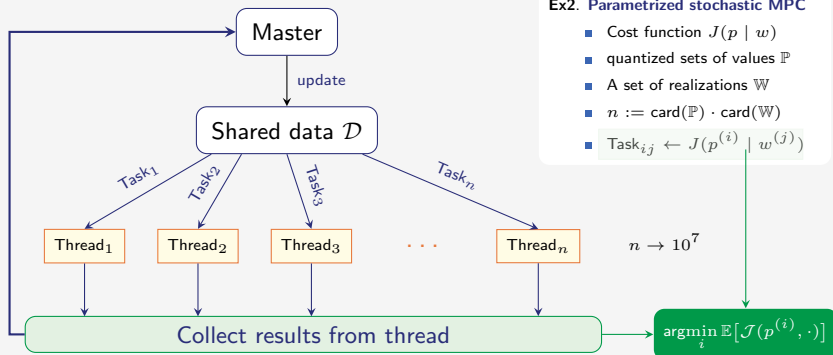
Ex2. Parametrized stochastic MPC

- Cost function $J(p | w)$
- quantized sets of values \mathbb{P}
- A set of realizations \mathbb{W}
- $n := \text{card}(\mathbb{P}) \cdot \text{card}(\mathbb{W})$
- $\text{Task}_{i,j} \leftarrow J(p^{(i)} | w^{(j)})$



DISTRIBUTING THE COMPUTATION

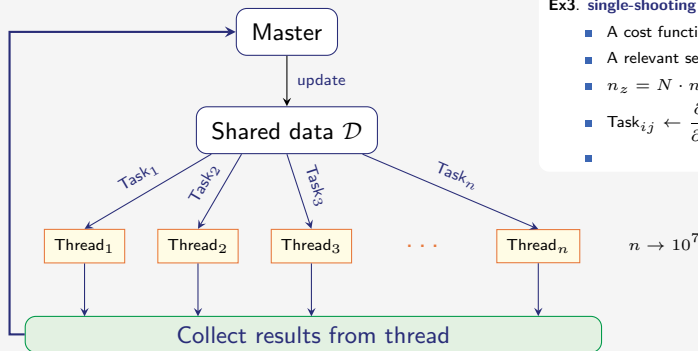
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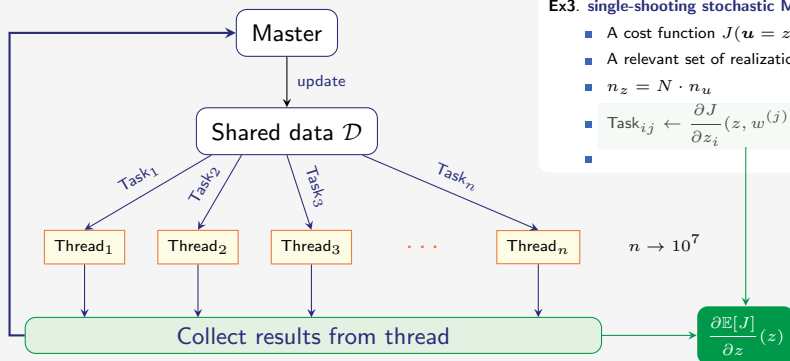


Ex3. single-shooting stochastic MPC

- A cost function $J(\mathbf{u} = \mathbf{z}, \mathbf{w})$
- A relevant set of realizations \mathbb{W}
- $n_z = N \cdot n_u$
- $\text{Task}_{ij} \leftarrow \frac{\partial J}{\partial z_i}(z, w^{(j)})$
-

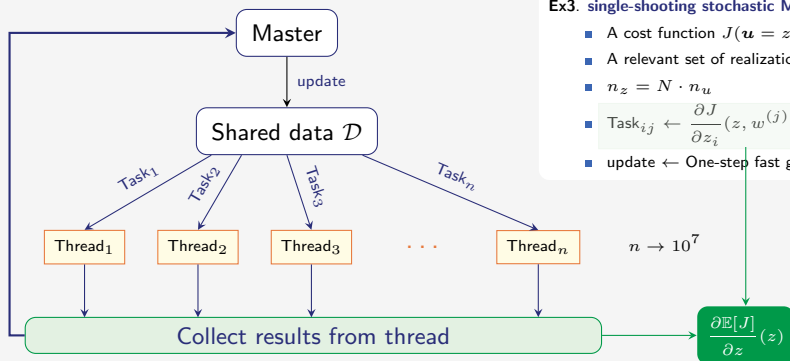
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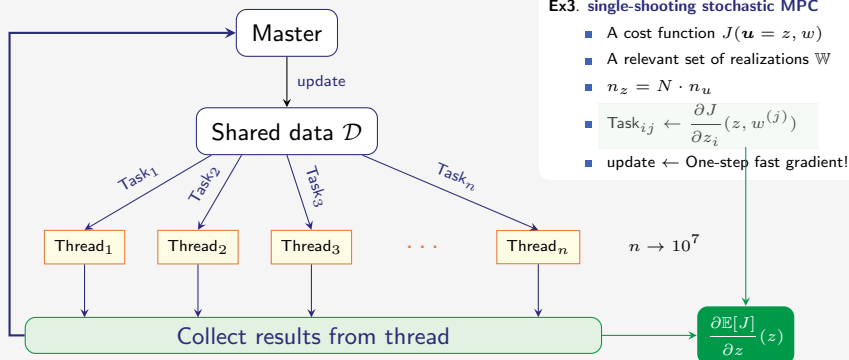


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- **update** \leftarrow One-step fast gradient!

DISTRIBUTING THE COMPUTATION

GPU, FPGA ...



https://colab.research.google.com/drive/1CJ14IaQ1s23D5Wn_6P-uIIzIgEfsr5ji?usp=sharing

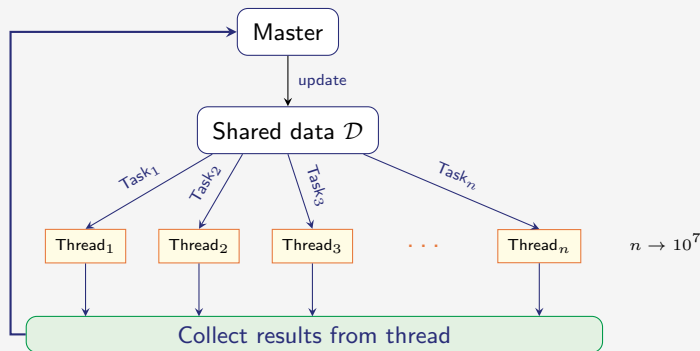
```
Number of scenarios = 20000
Prediction Horizon = 20
gpu computation time = 0.0002663135528564453
Number of individual tasks = 800000
```

```
t1 = time.time()
Grad(x0_gpu, U_gpu, W_gpu, J_gpu, G_gpu, mode_gpu,
    grid=(256, 16, 1), block=(256, 1, 1))
t2 = time.time()
```

Combined therapy
 $n_x = 4, n_w = 13$
 $n_u = 2, N = 20$

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GPU, FPGA ...



GPU-Based NMPC of a semi-active suspension

DISTRIBUTING THE COMPUTATION

GPU-Based MPC of a semi-active suspension.



K. M. M. Rathai



O. Sename

Half-Car SA-suspension

$$m_s \ddot{z}_s = -F_{s,\ell}(sa_\ell) - F_{s,r}(sa_r)$$

$$I_x \ddot{\theta} = \ell_\ell F_{s,\ell}(sa_\ell) - \ell_r F_{s,r}(sa_r)$$

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(ℓ) left, (r) right, (s) chassis, (t) wheel

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$$F_{t,i} = -k_{t,i}(z_{us,i} - z_{r,i}) \quad i \in \{\ell, r\}$$

Road profile ↙

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Road profile \leftarrow

$$sa_i = k_0 z_{d,i} + c_0 \dot{z}_{d,i} + f_c \phi_i \tanh(a_1 \dot{z}_{d,i} + a_2 z_{d,i})$$

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- Comfort ($\downarrow |\ddot{z}_s|$)
- Ride handling ($\downarrow |\ddot{\theta}^2|$)
- Box constraints on x/u

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$$\dot{x} = f(x, u, w), \quad (x, u, w) \in \mathbb{R}^8 \times \mathbb{R}^2 \times \mathbb{R}^2, \quad \tau_s \leq 5\text{msec}$$

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State of the art general NLP solver

- ACADO-qpOases / multiple shooting
- Symbolic automatic differentiation
- 4-th order Runge-Kutta integrator
- Code-generation based
- Standard p.w.c control profile
- projection of the quantized set
- Monitor the # iterations N_i

MATLAB/SIMULINK, Intel Core i7 PC

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$$F_{t,i} = -k_{t,i}(z_{us,i} - z_{r,i}) \quad i \in \{\ell, r\}$$

Road profile ↙

$$sa_i = k_0 z_{d,i} + c_0 \dot{z}_{d,i} + f_c \phi_i \tanh(a_1 \dot{z}_{d,i} + a_2 z_{d,i})$$

Control objective

- Comfort ($\downarrow |\ddot{z}_s|$)
- Ride handling ($\downarrow |\ddot{\theta}^2|$)
- Box constraints on x/u

Manipulated variables

- $u := (\phi_\ell, \phi_r) \in \mathbb{E}^2 \subset \mathbb{R}^2$
- \mathbb{E} is a quantized (discrete) set.

$$\dot{x} = f(x, u, w), (x, u, w) \in \mathbb{R}^8 \times \mathbb{R}^2 \times \mathbb{R}^2, \tau_s \leq 5\text{msec}$$

State of the art general NLP solver

- ACADO-qpOases / multiple shooting
- Symbolic automatic differentiation
- 4-th order Runge-Kutta integrator
- Code-generation based
- Standard p.w.c control profile
- projection of the quantized set
- Monitor the # iterations N_i

GPU/Simulation based solver

- Constant profile
- Card(\mathbb{E})² possibilities
- **Each is simulated by a single thread**
- **If** \exists admissible solutions:
Take the cost minimizer
- **otherwise:**
Minimize the constraint violation

MATLAB/SIMULINK, Intel Core i7 PC NVIDIA GTX 1050 / 768 CUDA cores

DISTRIBUTING THE COMPUTATION

GPU-Based MPC of a semi-active suspension.



K. M. M. Rathai



O. Sename

(FA) Feasibility
(CT) Computation Time
(NCLO) Normalized Closed-Loop Objective
(N_i) number of Newton iterations
(n_ϕ) card(\mathbb{E})

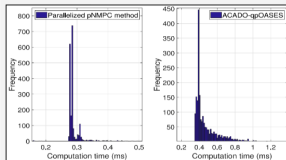
TABLE I
ACADO-qPOASES NMPC CONTROLLER

N_i	FA	Mean CT (ms)	Max CT (ms)	NCLO
5	✗	0.70	1.6	—
10	✗	0.95	2.2	—
15	✓	1.3	2.9	0.6484
20	✓	1.5	3.0	0.6412
25	✓	1.9	3.9	0.6317

TABLE II
PARALLELIZED pNMPC METHOD

$\{n_{\phi_1}, n_{\phi_2}\}$	FA	Mean CT (ms)	Max CT (ms)	NCLO
{2, 2}	✓	0.35	0.62	0.4679
{4, 4}	✓	0.35	0.60	0.4640
{8, 8}	✓	0.35	0.61	0.4646
{16, 16}	✓	0.36	0.55	0.4588
{32, 32}	✓	0.41	0.67	0.4568

(Courtesy K. M. M. Rathai)



(Courtesy K. M. M. Rathai)

$$sa_i = k_0 z_{d,i} + c_0 \dot{z}_{d,i} + f_c \phi_i \tanh(a_1 \dot{z}_{d,i} + a_2 z_{d,i})$$

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K. M. M. Rathai et al., GPU-based parametrized NMPC scheme ... IEEE Control Systems Letters, Vol. 3, Number 3, 2019

- 1 Non conventional NMPC Formulations
- 2 GPU-related topics
- 3 Machine Learning-related topics**
- 4 Discussion: Threats & suggestions for a data-dominated future

STOCHASTIC MPC USING SUPERVISED CLUSTERING

Distributing the data building over the real-life time

Dynamics $\dot{x} = f(x, u, w)$

Cost $J(\mathbf{u}|(x, w))$

Constraints $g(\mathbf{u}|(x, w))$

w-statistics \mathcal{W}

M.A On the use of supervised clustering in stochastic NMPC design. IEEE-TAC. Volume 65, Issue 12, 2020.

STOCHASTIC MPC USING SUPERVISED CLUSTERING

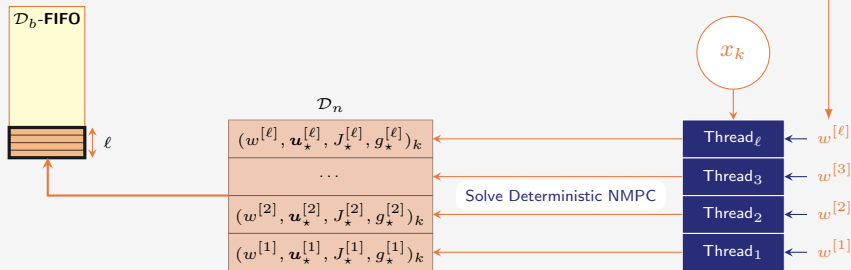
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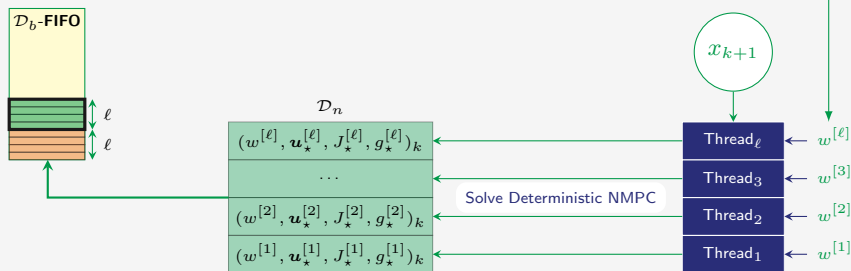
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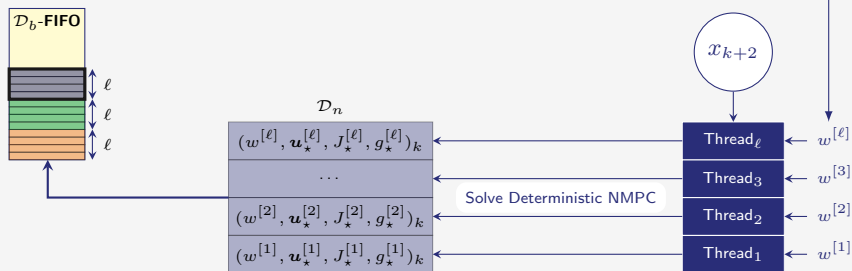
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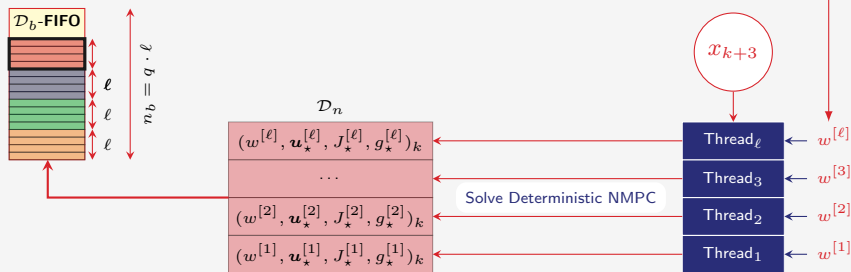
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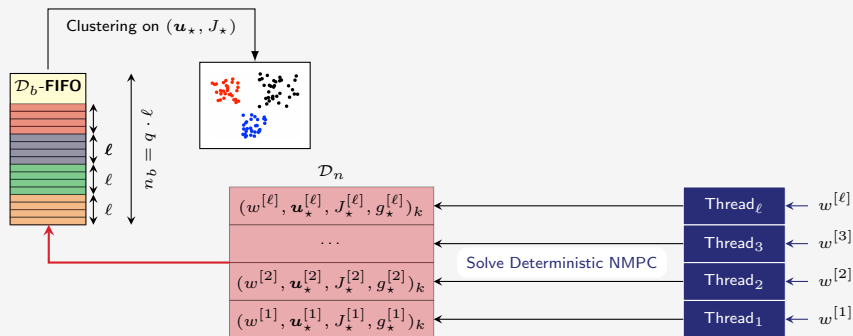
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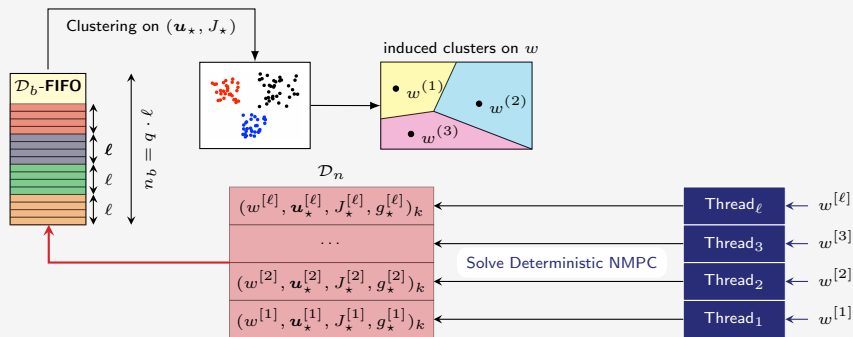
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Constraints $g(u|(x, w))$

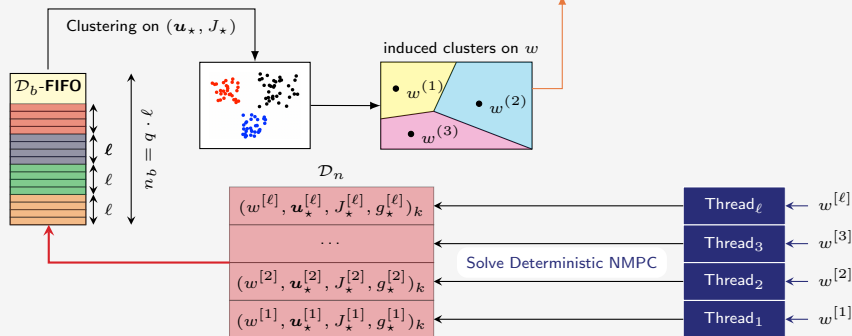
w-statistics \mathcal{W}

$$\min_{\mathbf{u}, \mu \geq 0} \sum_{i=1}^{n_{cl}} p_i \cdot J(\mathbf{u} | (x, w^{(i)}))$$

under

$$g(\mathbf{u} | (x, w^{(i)})) + \frac{1 - \epsilon}{\epsilon} \sigma_g^{(i)} \leq \mu$$

$$i = 1, \dots, n_{cl}$$



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$$i = 1, \dots, n_{cl}$$

x_1 tumor cell population;
 x_2 circulating lymphocytes population;
 x_3 chemotherapy drug concentration;
 x_4 effector immune cell population;
 u_1 rate of introduction of immunotherapy drug;
 u_2 rate of introduction of chemotherapy drug.

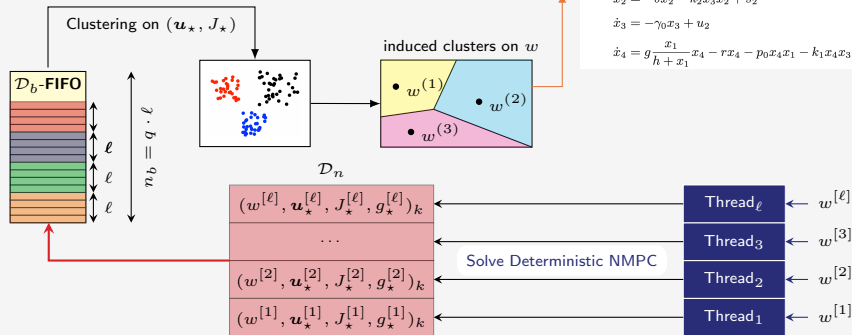
and the dynamics is given by

$$\dot{x}_1 = ax_1(1 - bx_1) - c_1x_4x_1 - k_3x_3x_1$$

$$\dot{x}_2 = -\delta x_2 - k_2x_3x_2 + s_2$$

$$\dot{x}_3 = -\gamma_0x_3 + u_2$$

$$\dot{x}_4 = g \frac{x_1}{h + x_1} x_4 - rx_4 - p_0x_4x_1 - k_1x_4x_3 + s_1u_1.$$



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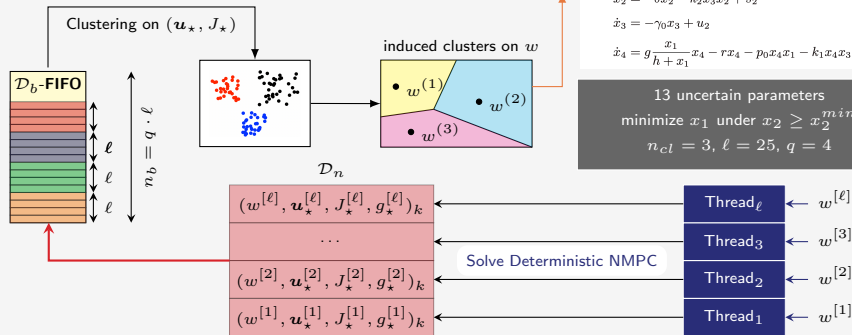
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13 uncertain parameters

minimize x_1 under $x_2 \geq x_2^{min}$

$n_{cl} = 3, \ell = 25, q = 4$



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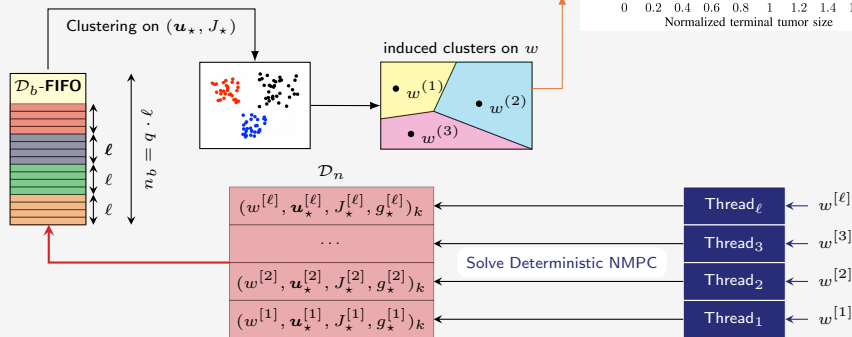
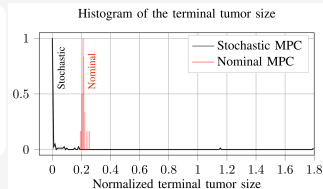
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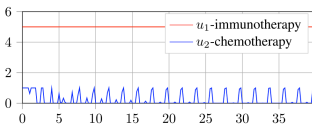
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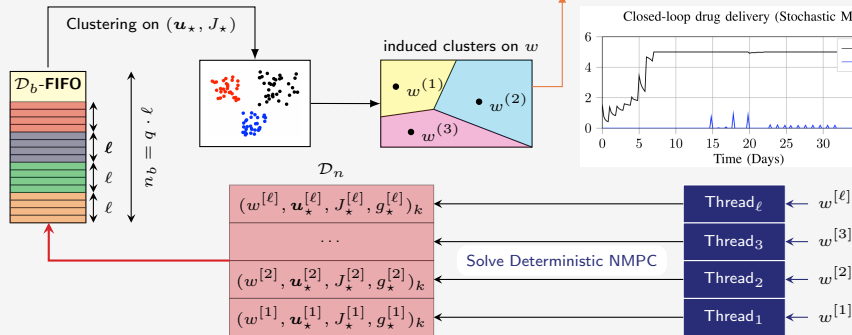
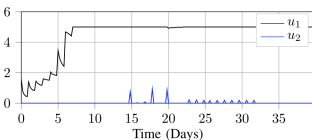
$$g(\mathbf{u}|(x, w^{(i)})) + \frac{1 - \epsilon}{\epsilon} \sigma_g^{(i)} \leq \mu$$

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Closed-loop drug delivery (Nominal MPC)



Closed-loop drug delivery (Stochastic MPC)



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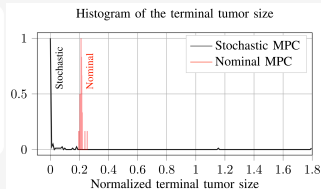
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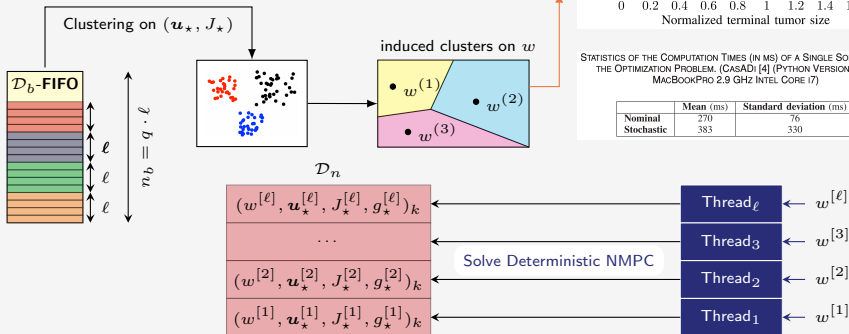
$$g(u|(x, w^{(i)})) + \frac{1 - \epsilon}{\epsilon} \sigma_g^{(i)} \leq \mu$$

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STATISTICS OF THE COMPUTATION TIMES (IN MS) OF A SINGLE SOLUTION OF THE OPTIMIZATION PROBLEM. (CASADI [4] (PYTHON VERSION) ON A MACBOOKPRO 2.9 GHZ INTEL CORE I7)

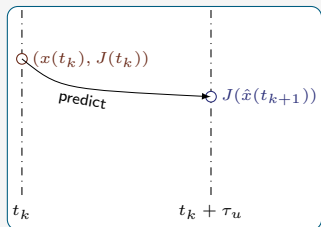
	Mean (ms)	Standard deviation (ms)
Nominal	270	76
Stochastic	383	330



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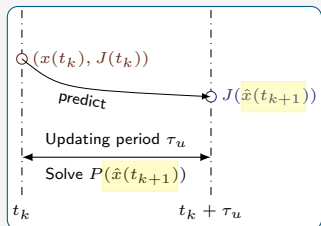
MONITORING CONTROL UPDATING PERIOD

New ML-induced opportunities (preliminary)



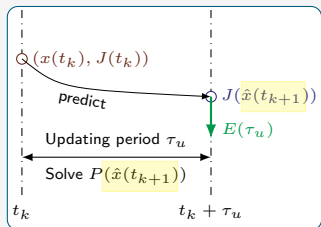
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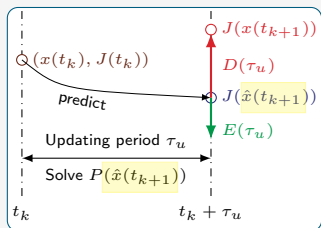
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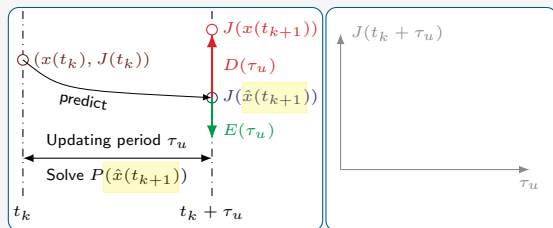
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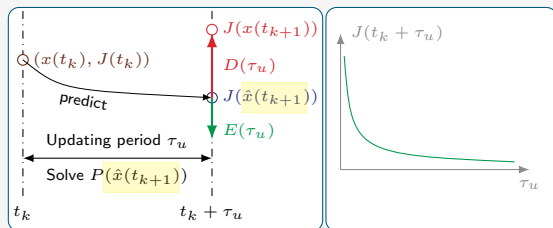
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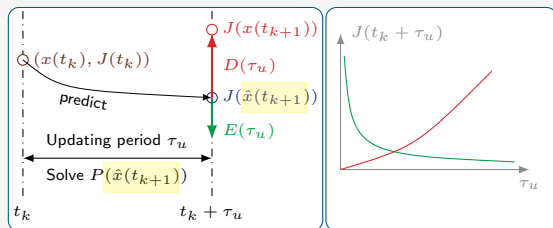
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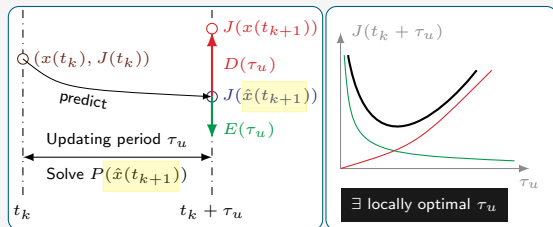
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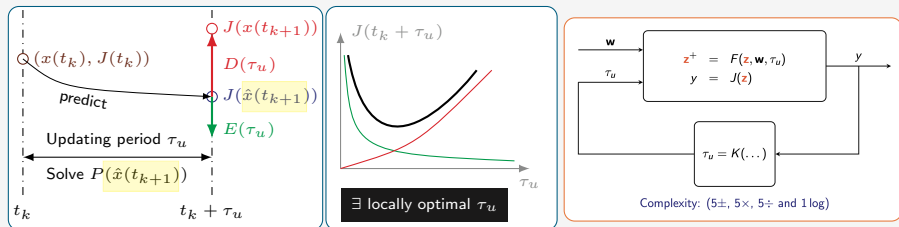
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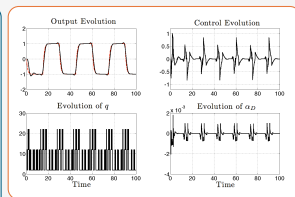
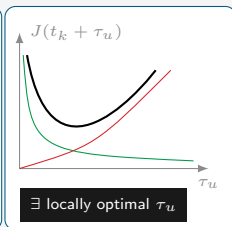
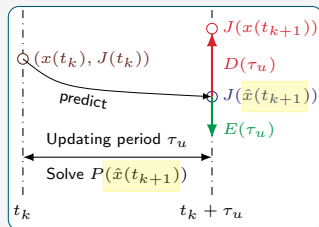
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M.A. Monitoring Control Updating Period In Fast Gradient-Based NMPC. ECC2013, 2013

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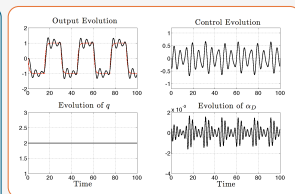
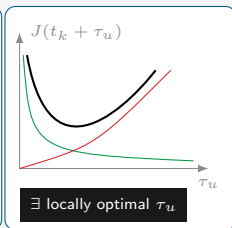
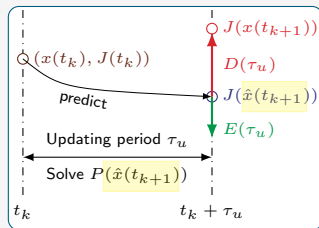


$\tau_u := q \times \text{cpu of a single iteration}$

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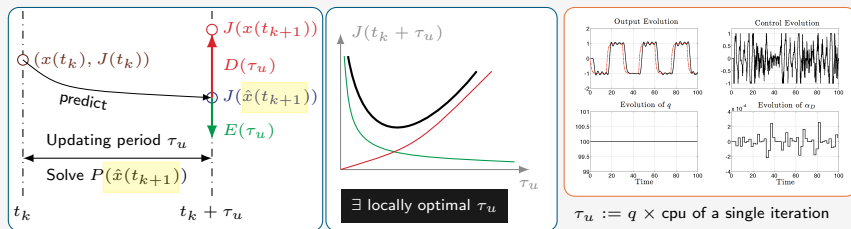


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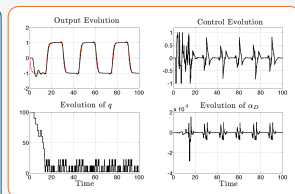
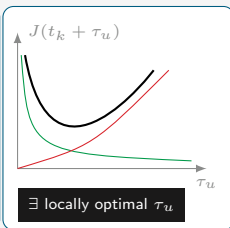
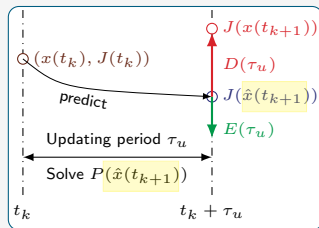
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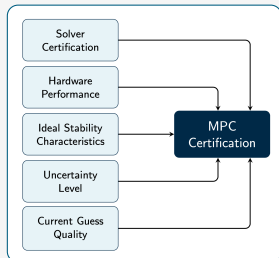
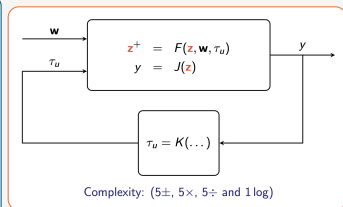
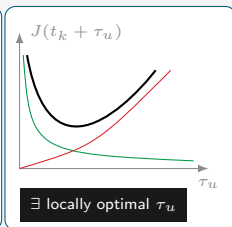
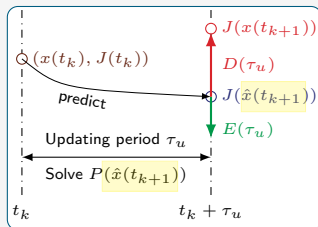


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M.A. Monitoring Control Updating Period In Fast Gradient-Based NMPC. ECC2013, 2013

MONITORING CONTROL UPDATING PERIOD

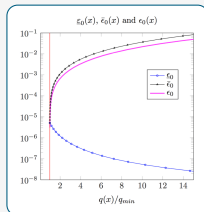
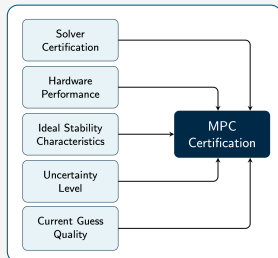
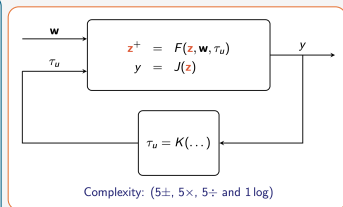
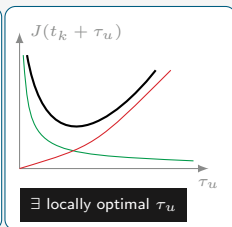
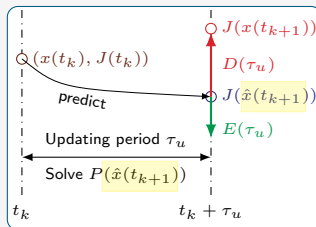
New ML-induced opportunities (preliminary)



M. Alamir. A State-Dependent Updating Period For Certified Real-Time MPC. IEEE TAC, 2017.

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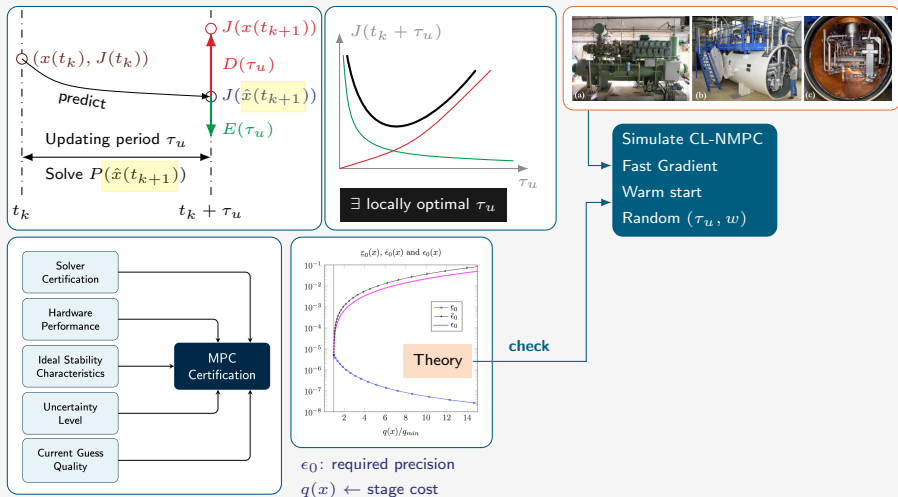


ϵ_0 : required precision
 $q(x) \leftarrow$ stage cost

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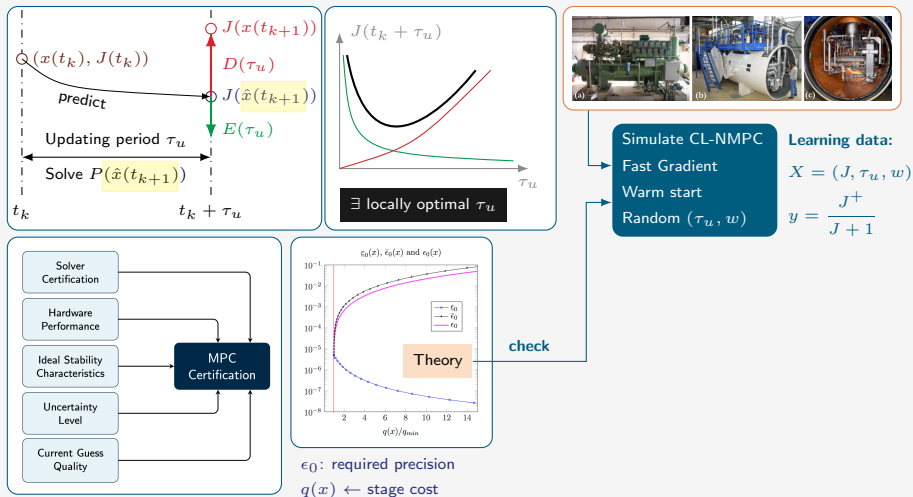
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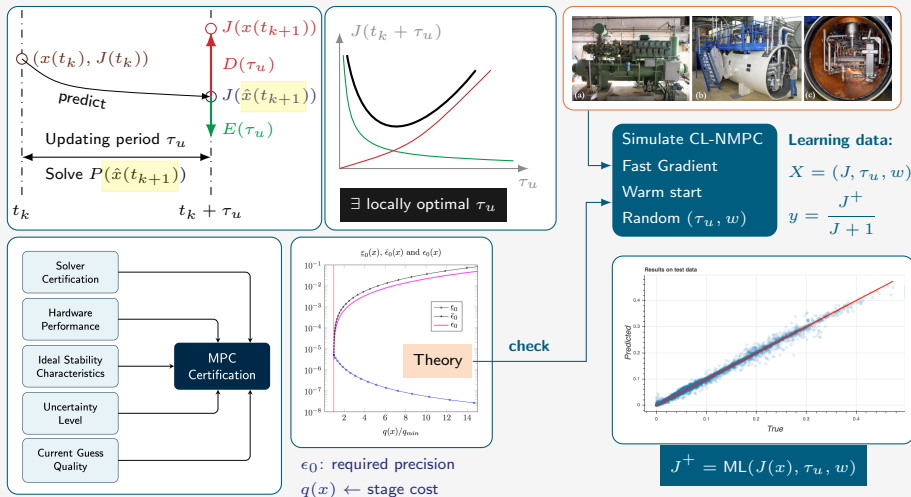
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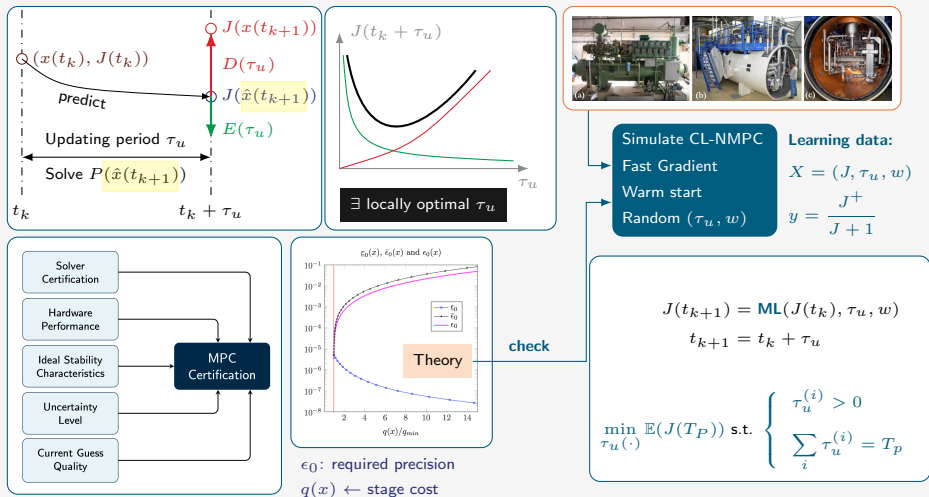
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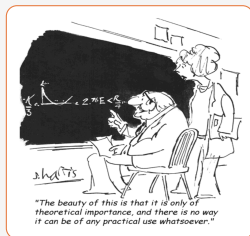
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- 1 Non conventional NMPC Formulations
- 2 GPU-related topics
- 3 Machine Learning-related topics
- 4 Discussion: Threats & suggestions for a data-dominated future

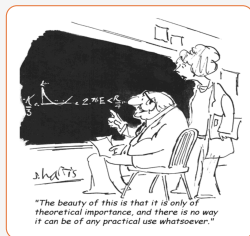
CONCLUSION



Control



CONCLUSION

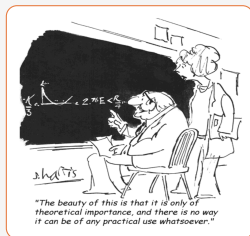


Control

Machine Learning



CONCLUSION



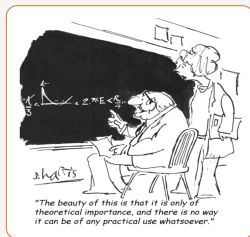
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Computational technologies
GPU, FPGA, Containers, ...

CONCLUSION



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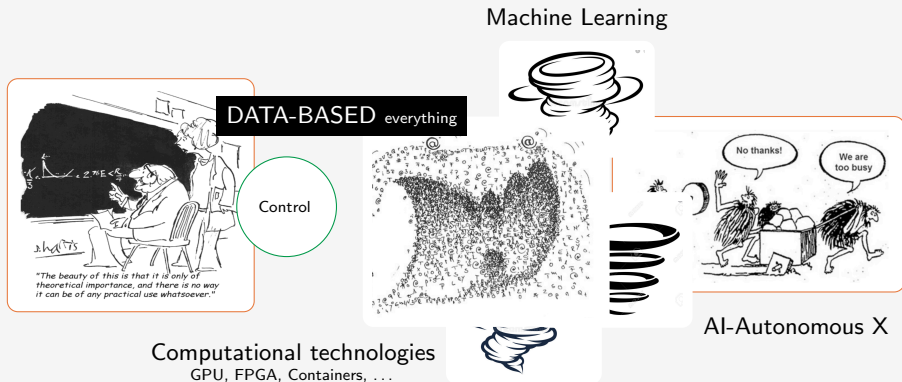
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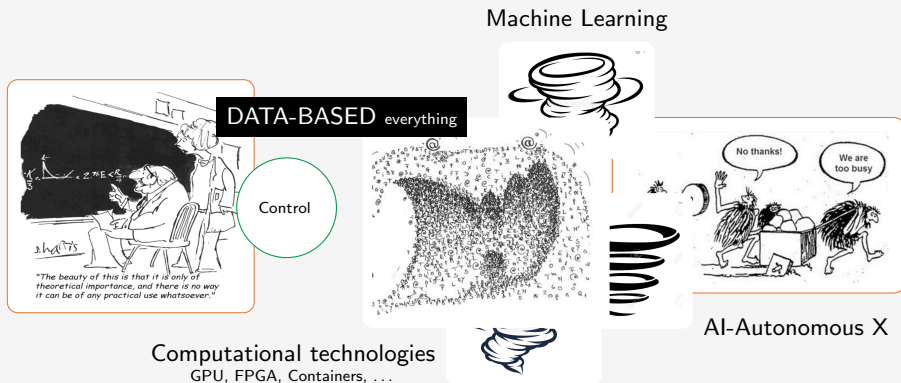
AI-Autonomous X

CONCLUSION



CONCLUSION

Business as usual is not an option!



Threat: Recycling old recipes ...

Finding a solution to a real-life problem with provable qualities



Exhibiting sufficient conditions for such a solution to exist.

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Finding a solution to a real-life problem with provable qualities



Exhibiting sufficient conditions for such a solution to exist.

- Once such **conditional** claims are published ...
- Nobody recalls the **unrealistic** supporting assumptions
- The absence of proofs is opposed to excellent heuristics that would efficiently solve **infinitely wider class** of real-life problems
- This was already nuisible in the past
- It is even more today as other actors (including giants) are working towards efficient and generic solutions

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Suggestions ...

- 1 Avoid problems for which we already got solutions (including models)
- 2 Build shared Blind, really challenging & realistic benchmarks
- 3 Systematically evaluate the cost of the learning phase (ex. RL)
- 4 Invest on automated generation of physically meaningful and control-oriented models
- 5 Share codes!

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Take home message . . .

We have assets & strengths!

Let's avoid to get lost in Random Forests! :-)

Keep critical and focus on the right fights!

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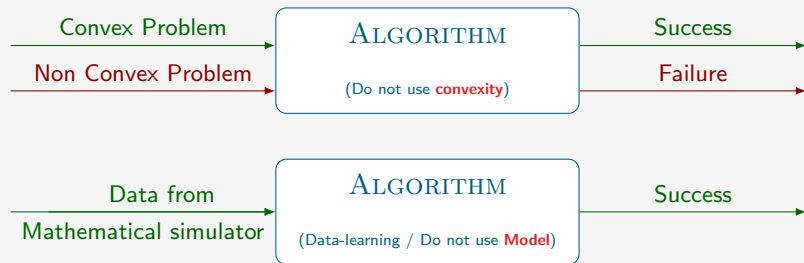
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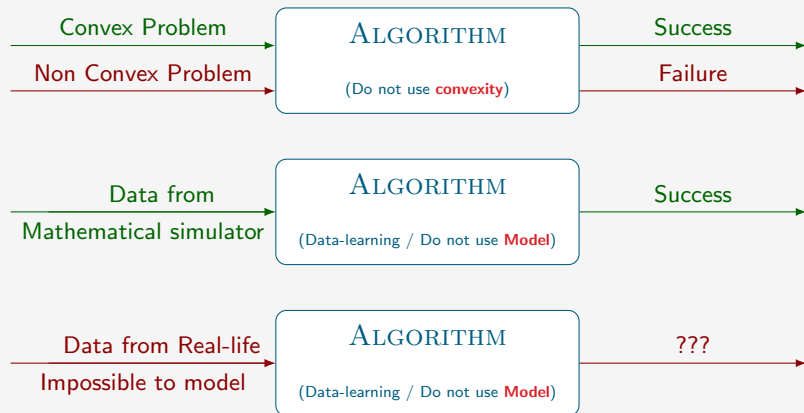
Conjecture



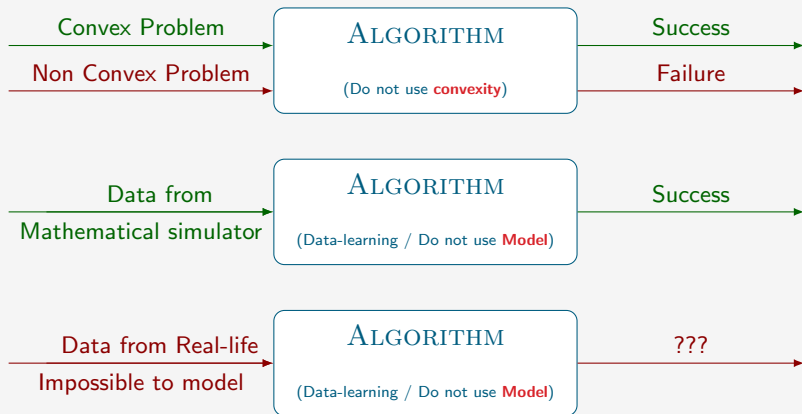
Conjecture



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What if (Success) \Leftrightarrow (\exists model)?